EE 435

Lecture 26

Data Converter Performance Characterization

Review from last lecture

Performance Characterization of Data Converters

- Static characteristics
 - Resolution
 - Least Significant Bit (LSB)
 - Offset and Gain Errors
 - Absolute Accuracy
 - Relative Accuracy
 - Integral Nonlinearity (INL)
 - Differential Nonlinearity (DNL)
 - Monotonicity (DAC)
 - Missing Codes (ADC)
 - Low-f Spurious Free Dynamic Range (SFDR)
 - Low-f Total Harmonic Distortion (THD)
 - Effective Number of Bits (ENOB)
 - Power Dissipation

Review from last lecture

Performance Characterization of Data Converters

- Dynamic characteristics
 - Conversion Time or Conversion Rate (ADC)
 - Settling time or Clock Rate (DAC)
 - Sampling Time Uncertainty (aperture uncertainty or aperture jitter)
 - Dynamic Range
 - Spurious Free Dynamic Range (SFDR)
 - Total Harmonic Distortion (THD)
 - Signal to Noise Ratio (SNR)
 - Signal to Noise and Distortion Ratio (SNDR)
 - Sparkle Characteristics
 - Effective Number of Bits (ENOB)

Review from last lecture Performance Characterization

Offset (for DAC)



- Offset strongly (totally) dependent upon performance at a single point
- Probably more useful to define relative to a fit of the data

Performance Characterization Offset (for DAC)



Offset relative to fit of data

Performance Characterization Offset (for DAC)



Though usually more useful, not standard (more challenging to test)

Performance Characterization Gain and Gain Error

For DAC



Gain error determined after offset is subtracted from output

Performance Characterization Offset

For ADC the offset is (assuming \mathcal{X}_{LSB} is the ideal first transition point)



(If ideal first transition point is not \mathscr{X}_{LSB} , offset is shift from ideal)

Performance Characterization Offset

For ADC the offset is



- Offset strongly (totally) dependent upon performance at a single point
- Probably more useful to define relative to a fit of the data

Performance Characterization Offset

For ADC the offset is



Offset relative to fit of data

Performance Characterization Gain and Gain Error



Gain error determined after offset is subtracted from output

Performance Characterization

Gain and Offset Errors

- Fit line would give better indicator of error in gain but less practical to obtain in test
- Gain and Offset errors of little concern in many applications
- Performance characteristic of interest often nearly independent of gain and offset errors
- Can be trimmed in field if gain or offset errors exist.











- INL is often the most important parameter of a DAC
- INL_0 and INL_{N-1} are 0 (by definition)
- There are N-2 elements in the set of INL_k that are of concern
- INL is almost always nominally 0 (i.e. designers try to make it 0)
- INL is a random variable at the design stage
- INL_k is a random variable for 0<k<N-1
- INL_k and INL_{k+j} are almost always correlated for all k,j (not incl 0, N-1)
- Fit Line is a random variable
- INL is the N-2 order statistic of a set of N-2 correlated random variables



- At design stage, INL characterized by standard deviation of the random variable
- Closed-form expressions for INL almost never exist because PDF of order statistics of correlated random variables is extremely complicated
- Simulation of INL very time consuming if n is very large (large sample size required to establish reasonable level of confidence)
 - Model parameters become random variables
 - Process parameters affect multiple model parameters causing model parameter correlation
 - Simulation times can become very large
- INL can be readily measured in laboratory but often dominates test costs because of number of measurements needed when n is large
- Expected value of INL_k at k=(N-1)/2 is largest for many architectures
- Major effort in DAC design is in obtaining acceptable INL yield !

How many bits in this DAC? How many bits in this ADC?



Could even have random number generator generating 4 MSBs in this ADC

Manufacturers can "play games" with characterizing data converters

That is one of the major reasons it is not sufficient to simply specify the number of bits of resolution to characterize data converters !

- Concept of Equivalent Number of Bits (ENOB) is to assess performance of an actual DAC to that of an ideal DAC at an "equivalent" resolution level
- Several different definitions of ENOB exist for a DAC
- Here will define ENOB as determined by the actual INL performance
- Will use subscript to define this ENOB, e.g. ENOB_{INL}

Thus define the effective number of bits, n_{EFF} by the expression

Thus, if an n-bit DAC has an INL of 1/2 LSB

$$ENOB_{INL} = \log_2\left(\frac{V_{REF}}{INL}\right) - 1 = \log_2\left(\frac{2^n V_{LSB}}{\frac{V_{LSB}}{2}}\right) - 1 = \log_2\left(2^{n+1}\right) - 1 = n$$

Note: With this definition, an n-bit DAC could actually have an ENOB_{INI} larger than n

Integral Non-Linearity (INL) Integral Non-Linearity Integral Non-Linearity (INL) is defined as the Conversion sum from the first to the current conversion \$7 (integral) of the non-linearity at each code Adjusted Transfer (Code DNL). For example, if the sum of the Function (Dashed) \$6 DNL up to a particular point is 1LSB, it means \$5 Ideal Transfer unction (dotted) INL = 0.0the total of the code widths to that point is \$4 1LSB greater than the sum of the ideal code \$3 widths. Therefore, the current point will \$2 INL = +0.50 convert one code lower than the ideal \$1 = +0.25conversion. \$0 2 3 5 6 VREFL In more fundamental terms, INL represents Input Voltage in LSB the curvature in the Actual Transfer Function relative to a baseline transfer function or the difference between the current and the ideal transition voltages. There are three primary definitions of INL in common use. They all have the same fundamental definition except they are measured against different transfer functions. This fundamental definition is:

Semicon

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Code INL = V(Current Transition) – V(Baseline Transition) INL = Max(Code INL)

ADC Definitions and Specifications

For More Information On This Product, Go to: www.freescale.com

Actually probably more than 3

Consider end-point fit line with interpreted output axis

$$X_{\text{INF}}(\mathcal{X}_{\text{IN}}) = m\mathcal{X}_{\text{IN}} + \left(\frac{\mathcal{X}_{\text{LSB}}}{2} - m\mathcal{X}_{\text{T1}}\right)$$
$$m = \frac{(N-2)\mathcal{X}_{\text{LSB}}}{\mathcal{X}_{\text{T7}} - \mathcal{X}_{\text{T1}}}$$

Continuous-input based INL definition

Continuous-input based INL definition

Often expressed in LSB

$$\mathsf{INL}(\mathfrak{X}_{\mathsf{IN}}) = \frac{\tilde{\mathfrak{X}}_{\mathsf{IN}}(\mathfrak{X}_{\mathsf{IN}}) - \mathsf{X}_{\mathsf{INF}}(\mathfrak{X}_{\mathsf{IN}})}{\mathfrak{X}_{\mathsf{LSB}}}$$
$$\mathsf{INL} = \max_{0 \le \mathfrak{X}_{\mathsf{IN}} \le \mathfrak{X}_{\mathsf{REF}}} \left\{ |\mathsf{INL}(\mathfrak{X}_{\mathsf{IN}})| \right\}$$

Nonideal ADC

With this definition of INL, the INL of an ideal ADC is $\mathcal{X}_{LSB}/2$ (for $\mathcal{X}_{T1}=\mathcal{X}_{LSB}$)

This is effective at characterizing the overall nonlinearity of the ADC but does not vanish when the ADC is ideal and the effects of the breakpoints are not explicit

Nonideal ADC

Break-point INL definition (most popular)

Place N-3 uniformly spaced points between X_{T1} and X_{T(N-1)} designated \mathcal{X}_{FTk} INL_k= \mathcal{X}_{Tk} - \mathcal{X}_{FTk} 1 ≤ k ≤ N-2 INL = $\max_{2 \le k \le N-2} \{|INL_k|\}$

Nonideal ADC

Break-point INL definition (assuming all break points present)

Nonideal ADC

Break-point INL definition

- INL is often the most important parameter of an ADC
- INL_1 and INL_{N-1} are 0 (by definition)
- There are N-3 elements in the set of INL_k that are of concern
- INL is a random variable at the design stage
- INL_k is a random variable for 0<k<N-1
- INL_k and INL_{k+j} are correlated for all k,j (not incl 0, N-1) for most architectures
- Fit Line (for cont INL) and uniformly spaced break pts (breakpoint INL) are random variables
- INL is the N-3 order statistic of a set of N-3 correlated random variables (breakpoint INL)

Nonideal ADC

Break-point INL definition

- At design stage, INL characterized by standard deviation of the random variable
- Closed-form expressions for INL almost never exist because PDF of order statistics of correlated random variables is extremely complicated
- Simulation of INL very time consuming if n is very large (large sample size required to establish reasonable level of confidence)
 - -Model parameters become random variables
 - -Process parameters affect multiple model parameters causing model parameter correlation
 - -Simulation times can become very large

- Measuring INL in the laboratory based upon this definition would be totally impractical if n is very large
- A "Code Density" approach is often used in the laboratory to estimate the transition points without actually measuring them to dramatically reduce test costs
- INL can be readily measured in laboratory using Code Density approach but even this approach often dominates test costs because of number of measurements needed when n is large
- INL is a random variable and is a major contributor to yield loss in many designs
- Expected value of INL_k at k=(N-1)/2 is largest for many architectures
- This definition does not account for missing transitions
- Major effort in ADC design is in obtaining an acceptable yield

INL-based ENOB

Consider initially the continuous INL definition for an ADC where the INL of an ideal ADC is $X_{LSB}/2$

Assume

INL= vX_{LSBR}

where X_{LSBR} is the LSB based upon the defined resolution, n_{R}

$$NL = \frac{\upsilon X_{REF}}{2^{n_R}} = \frac{X_{REF}}{2^{n_{eq}+1}}$$
$$\upsilon = 1$$

Thus

$$\frac{\upsilon}{2^{n_{\mathsf{R}}}} = \frac{1}{2^{n_{eq}+1}}$$

But $ENOB_{INL} = n_{eq}$

Hence

ENOB =
$$n_R$$
-1-log₂(v)

INL-based ENOB ENOB = n_R -1-log₂(v)

Consider an ADC with specified resolution of n (dropped the subscript R) and INL of v LSB

U	ENOB
1/2	n
1	n-1
2	n-2
4	n-3
8	n-4
16	n-5

ENOB could be larger than n_R as well though with less transition levels

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Stay Safe and Stay Healthy !

End of Lecture 26